

we find $\rho_d > \rho_c$ for a closed universe, as expected; this greater density at ρ_d is offset by a greater value for H_d .)

H_d was for a given value of H_0 and ρ_0 that we found ρ_d, R_0 and R_d in a closed

universe. We put those values into the eq. $\frac{R_0}{R_d} = \left(\frac{t_0}{t_d}\right)^{2/3}$ (which applies to open

universe) to find t_0 . (Hence in part (iv) we mixed values found for critical and closed universes). Since deceleration is greater in a closed universe

than an open universe, H decreases faster as t increases (ie deceleration $q > 1/2$ is greater). Hence for a given value of H_0 , H_d would have been greater in a closed than an critical universe.

$$\text{since } \rho_d = N \left(H_d^2 + \frac{k c^2}{R_d^2} \right)$$

and H_d^2 is greater in a closed universe for a given value of H_0 we would expect ρ_d to be greater in a closed than a critical universe for this given value of H_0 .

In this case $\frac{k c^2}{R_d^2} \ll H_d^2$, and whether we put $k=0$ or 1 does not make much difference, but I worked $k=0$ out anyway in one of the other solutions.