

$$K = \frac{R^2}{c^2} \left( \frac{1.0001 \times 10^{-9} \text{ J/m}^3}{1.6077 \times 10^{26} \text{ kg m}^{-1}} - (2 \times 10^{-18} \text{ s}^{-1})^2 \right)$$

$$= \frac{2.2207 \cdot R^2}{c^2} \times 10^{-36} \text{ s}^{-2} > 0 \text{ since } R^2 > 0. \text{ see opposite for } R(t_0)$$

$K$  expresses qualitatively the curvature of spacetime:

If  $K=1$ , space and spacetime are positively curved, like the surface of a sphere (universe is closed).

If  $K=0$ , the spatial part of spacetime is flat like a plane is Euclidean. Universe is critical, but spacetime is not flat unless  $dR=0$ , which is never the case in a critical  $dt$  universe.

If  $K=-1$ , space and spacetime are negatively curved, like surface of a horn. Universe is open.

A quantitative measure of the curvature of space is given by  $\frac{1}{R^2}$ , a measure of

the Riemannian curvature of space.

If  $K=1$ ,  $R \rightarrow R_{\max}$  : curvature of space  $\rightarrow \frac{1}{R_{\max}^2}$

If  $K=-1$ ,  $R \rightarrow \infty$  : curvature of space  $\rightarrow \frac{1}{\infty^2} = 0$

If  $K=0$ , curvature of space  $= 0$

In all case curvature of space  $= 0$  or tends to 0 as  $R$  increases, though for a closed universe this is true only while  $R$  is increasing i.e.  $\frac{dR}{dt} > 0$