

Q17 **D**

Objects given: A free particle P with position  $x(t)$  in a non-inertial frame S.  
 To be found: The acceleration  $a(t)$  of P in S.  
 Direct solution: Take the second derivative of each component of  $x(t)$ .  
 Result: Item (D).  
 Corroboration: Items (A, B, C, G) cannot be right because the 1- and 2-components must be zero. Item (E) is out because the 3-component cannot depend on  $t$ . Item (F) is out when care is taken with the derivative. This leaves item (D).

Q18 **B**

Objects given: A different free particle P' with position  $x(t)$  in the non-inertial frame S.  
 To be found: Up to two expressions for  $x(t)$  which could describe the motion of P'.  
 Direct solution: Seek an equation yielding the same acceleration (second derivative) as the original.  
 Result: Item (B).  
 Corroboration: Items (C, D, E, F, G) are out because the 3-component has the wrong powers of  $t$ , and item (A) is out because it has the wrong sign.

Q19 **G**

Objects given: A free particle P with mass  $m$  and acceleration  $a(t)$  in a non-inertial frame S'.  
 To be found: The force needed to make P look free in S'.  
 Direct solution: Multiply  $a$  by  $m$  to yield the apparent force on P, and reverse the sign.  
 Result: Item (G).  
 Corroboration: Item (F) has the wrong sign, items (D, E) have forgotten  $m$ , item (A) has  $m$  in the denominator and items (B, C) have the wrong power of  $t$ . This leaves only item (G).

Q20 **C, E, F**

Objects given: All free particles in any non-inertial frame.  
 To be found: Up to three true statements about them.  
 Direct solution: Eliminate the absurd statements. That gets rid of items (A, B, D, G).  
 Result: Items (C, E, F).  
 Corroboration: Item (C) is true for free particles in a purely rotating non-inertial frame; item (E) is true by the analysis in Q18, item (F) is true since the particles have the same acceleration.

Q21 **F**

Objects given: A planet which has the same mean distance from its star as Earth has from the Sun, but which orbits twice as fast.  
 To be found: The mass of its star.  
 Direct solution:  $v^2/r = GmM/r^2$  so  $v^2$  is proportional to  $M/r$ .  
 Result: If  $v$  is doubled,  $v^2$  is quadrupled, so the mass of the star is four times that of Earth: item (F).  
 Corroboration: By Kepler's third law, planetary comparisons depend on the square of the orbital period.

Q22 **F**

Objects given: A second planet which is four times as far from its star as is the first.  
 To be found: The period  $T$  of its (circular) orbit.  
 Direct solution: By Kepler's third law,  $T^2/r^3$  is constant for any planetary system.  
 Result:  $T$  is eight times the period of the first planet: item (F).  
 Corroboration: From Q21,  $(rv^2)$  is a constant, so  $v$  for the second planet is cut in half while its orbit is four times as large.