

of length related to the cluster's radius, and the velocity dispersion is obtained from Doppler shifts (assuming gravitationally bound). Specifically

$$\sigma \propto \left(\frac{M}{R}\right)^{1/2} \quad \text{(P.S. I am told the virial theorem applies to all gravitationally bound systems. Yes)}$$

$$\frac{3}{15} M \propto R \sigma^2$$

To find R we need the angular diameter and the distance to the cluster

3) a) Using $2R = d$ where $2R$ is diameter of emitting region (upper limit), t is period of variation.

$$2R = ct = 3 \times 10^8 \text{ m/s} \times 20 \times 60 \text{ s}$$

Do not write like this use

$$= 3.6 \times 10^{11} \text{ m}$$

$$3.6 \times 10^{11} \text{ m}$$

$$\approx 1 \times 10^{-5} \text{ pc}$$

$$= \frac{3.6 \times 10^{11} \text{ m}}{3.09 \times 10^{16} \text{ m/pc}}$$

$$\frac{2 \times 10}{3} = 1.165 \times 10^{-5} \text{ parsec}$$

NOT 4 s.f.!

b) $2R = d$

$$= 3 \times 10^8 \text{ m/s} \times 2 \times 3600 \text{ s}$$

$$= 2.16 \times 10^{12} \text{ m}$$

$$\text{or } \frac{2.16 \times 10^{12} \text{ m}}{3.09 \times 10^{16} \text{ m/pc}} = 7.0 \times 10^{-5} \text{ pc}$$

$$7 \times 10^{-5} \text{ pc}$$

You must use standard convention in writing powers of 10

c) The infrared emitting region is likely to be larger than the X-ray emitting region. Infrared radiation originates mainly from the dust/gas surrounding the AGN, while the X-ray originates