

E is wrong; other elements beside titanium have $A = 60$ (eg. $^{60}_{27}\text{Co}$, an unstable isotope of Cobalt), but the different number of protons (the Z number) leads to a different potential energy function and different energy levels.

F is wrong; all titanium isotopes have the same number of protons in the nucleus.

G is wrong; see answer to C; $l = 3$ corresponds to an f state and these are not occupied in the ground state.

Q15 The correct options are D and E

The first ionisation energy is the energy required to remove the least tightly bound electron. The electron configuration of rubidium is $1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6 5s$ ($Z = 37$, and $5s$ shell fills before $4d$ shell; see Table 8 and Figure 20 of Unit 15). The electron in the $5s$ state is the least tightly bound.

Q16 A and F are correct

These particles are bosons. If particles contain an *odd* number of fermions, they are therefore themselves fermions, and obey the generalised exclusion principle. If particles contain an *even* number of fermions, they are bosons and do *not* obey the generalised exclusion principle.

CO is a boson, since it contains an even number of fermions (14 protons + 14 electrons + 14 neutrons)

^3_2He is a fermion (2 protons + 2 electrons + 1 neutron)

NO is a fermion (15 protons + 15 electrons + 15 neutrons)

^9_4Be is a fermion (4 protons + 4 electrons + 5 neutrons)

$^{14}_7\text{N}$ is a fermion (7 protons + 7 electrons + 7 neutrons)

^7_3Li is a boson (3 protons + 3 electrons + 4 neutrons)

BeO is a fermion (12 protons + 12 electrons + 13 neutrons)

Q17 The correct response is F

A is irrelevant because the photons in laser light are bosons, so they do not obey an exclusion principle.

B is also not relevant; ^4He atoms are bosons, thus having the positive tendency to share the same quantum state.

C is not the correct response; although tunnelling is a purely quantum mechanical effect, it has no *direct* relation to the Pauli exclusion principle which is the concern of this question.

D is irrelevant because the wave-like properties that lead to diffraction are a consequence of de Broglie's equation which applies whether the particles involved are bosons or fermions.

E is also irrelevant; the quantum mechanical phenomenon of tunnelling is not directly relevant here.

F is correct; it is the Pauli pressure created by the electrons (fermions) which resists the collapse of the core of a red giant, thus forming a stable entity called a white dwarf.

G is irrelevant because these instabilities are thought to be due to a sudden transfer of angular momentum from the surface and a superfluid region inside the neutron star.

Q18 The correct answer is E

According to Unit 16,

$$E_{\max} = \frac{h^2 (N/V)^{2/3}}{8m_e}$$

$$\text{so } \frac{N}{V} = \left(\frac{E_{\max} \times 8m_e}{h^2} \right)^{3/2} = \left(\frac{8.0 \times 10^{-11} \text{ J} \times 8 \times 9.11 \times 10^{-31} \text{ kg}}{(6.63 \times 10^{-34} \text{ J s})^2} \right)^{3/2}$$

$$= 4.83 \times 10^{40} \text{ m}^{-3}$$

$$\text{Hence } P = \frac{2}{3} \frac{N}{V} \times \frac{3}{5} E_{\max} = \frac{2}{5} \frac{N}{V} E_{\max}$$

$$= \frac{2}{5} \times 4.83 \times 10^{40} \text{ m}^{-3} \times 8.0 \times 10^{-11} \text{ J} = 1.5 \times 10^{30} \text{ N m}^{-2}$$

(Note that $1 \text{ J m}^{-3} = 1 \text{ N m}^{-2}$ because $1 \text{ J} = 1 \text{ N m}$).