radius of convergence is 1

c) The series will terminate after a finite number of terms (the one with B's).

Since they contains factors $(n(n+1) - \alpha(\alpha+1))$ so when $n=\alpha$ subsequent terms will vanish.