

$$H(q, p, t) = H_0(q, p) + \epsilon q \sin \Omega t$$

$$= \frac{p^2}{2} + V(q) + \epsilon q \sin \Omega t$$

$$\dot{q} = \frac{\partial H}{\partial p} = p$$

$$\dot{p} = -\frac{\partial H}{\partial q} = -V'(q) - \epsilon \sin \Omega t \quad \checkmark$$

$$G = \begin{pmatrix} p \\ -V'(q) \end{pmatrix} \quad \checkmark \quad G_1 = p$$

$$G_2 = -V'(q)$$

$$P = \begin{pmatrix} 0 \\ -\sin \Omega t \end{pmatrix} \quad \checkmark \quad P_1 = 0$$

$$P_2 = -\sin \Omega t$$

Using Melnikov's

$$M(t_0) = \int_{-\infty}^{\infty} \{G_1(\tau)P_2(\tau, \tau+t_0) - G_2(\tau)P_1(\tau, \tau+t_0)\} d\tau$$

$$= \int_{-\infty}^{\infty} \{p(\tau) \cdot -\sin \Omega(\tau+t_0) - (-V'(q(\tau)) \cdot 0\} d\tau$$

$$= -\int_{-\infty}^{\infty} p(\tau) \sin \Omega(\tau+t_0) d\tau \quad \checkmark$$

$$= -\int_{-\infty}^{\infty} p(\tau) (\sin \Omega \tau \cos \Omega t_0 + \cos \Omega \tau \sin \Omega t_0) d\tau$$

$$= -\int_{-\infty}^{\infty} p(\tau) \sin \Omega \tau \cos \Omega t_0 d\tau - \int_{-\infty}^{\infty} p(\tau) \cos \Omega \tau \sin \Omega t_0 d\tau$$

$$= -\cos \Omega t_0 \int_{-\infty}^{\infty} p(\tau) \sin \Omega \tau d\tau - \sin \Omega t_0 \int_{-\infty}^{\infty} p(\tau) \cos \Omega \tau d\tau$$

Assuming
time is
measured
from pt where
these fns
are so

$p(\tau), \sin \Omega \tau$ are both odd. \checkmark
 $\therefore -p(\tau) \sin \Omega \tau$ is even \checkmark

$\cos \Omega \tau$ is even $\therefore p(\tau) \cos \Omega \tau$ is odd
 $\therefore \int_{-\infty}^{\infty} p(\tau) \cos \Omega \tau d\tau = -\int_{-\infty}^{\infty} p(\tau) \cos \Omega \tau d\tau$

$$\int_{-\infty}^{\infty} p(\tau) \cos \Omega \tau d\tau = 0$$

$$\therefore M(t_0) = -\cos \Omega t_0 \int_{-\infty}^{\infty} p(\tau) \sin \Omega \tau d\tau \quad \checkmark$$

$$= -2 \cos \Omega t_0 \int_0^{\infty} p(\tau) \sin \Omega \tau d\tau \neq 0$$