

$$L \quad 4) H(q, p) = \frac{p^2}{2(1+a \sin q)} - \cos q$$

$$\dot{q} = \frac{\partial H}{\partial p} = \frac{\partial}{\partial p} \left(\frac{p^2}{2(1+a \sin q)} - \cos q \right)$$

$$= \frac{p}{(1+a \sin q)}$$

$$\frac{\partial^2 H}{\partial p^2} = \frac{\partial}{\partial p} \left(\frac{p}{(1+a \sin q)} \right) = \frac{1}{1+a \sin q}$$

$$\dot{p} = -\frac{\partial H}{\partial q} = -\frac{\partial}{\partial q} \left(\frac{p^2}{2(1+a \sin q)} - \cos q \right) \quad \checkmark$$

$$= \frac{+a p^2 \cos q}{2(1+a \sin q)^2} - \sin q$$

$$\frac{\partial^2 H}{\partial q^2} = \frac{\partial}{\partial q} \left(\frac{+a p^2 \cos q}{2(1+a \sin q)^2} - \sin q \right)$$

$$= \left(\frac{2(1+a \sin q)^2 \frac{\partial}{\partial q} (+a p^2 \cos q)}{\partial q} \right)$$

$$- \left(+a p^2 \cos q \right) \frac{\partial}{\partial q} (2(1+a \sin q)^2) \quad \checkmark$$

$$= \frac{4(1+a \sin q)^4}{\partial q}$$

$$= \frac{-2(1+a \sin q)^2 a p^2 \sin q - 4 a^2 p^2 \cos^2 q (1+a \sin q)}{4(1+a \sin q)^4}$$

$$= \frac{-(1+a \sin q) a p^2 \sin q - 2 a^2 p^2 \cos^2 q + \cos q}{2(1+a \sin q)^3}$$

$$= \frac{-a p^2 \sin q - a^2 p^2 \cos^2 q - a^2 p^2 + \cos q}{2(1+a \sin q)^3}$$

$$\frac{\partial^2 H}{\partial q \partial p} = \frac{\partial}{\partial q} \left(\frac{\partial H}{\partial p} \right) = \frac{\partial}{\partial q} \left(\frac{p}{(1+a \sin q)} \right)$$

$$= \frac{-a p \cos q}{(1+a \sin q)^2}$$

At the fixed points, $\dot{p} = \dot{q} = 0$