

(4)

$$\begin{aligned}
 &= \frac{-\frac{1}{16}(x^2+2x-3) + \frac{1}{4}(x+3) + \frac{1}{16}(x^2-2x+1)}{(x-1)^2(x+3)} \\
 &= \frac{x^2(-\frac{1}{16} + \frac{1}{16}) + x(-\frac{2}{16} + \frac{4}{16} - \frac{2}{16}) + (\frac{3}{16} + \frac{12}{16} + \frac{1}{16})}{(x-1)^2(x+3)} \\
 &= \frac{0+0+1}{(x-1)^2(x+3)} = \frac{1}{(x-1)^2(x+3)} \checkmark
 \end{aligned}$$

Integral becomes

$$\begin{aligned}
 \int_0^t dx &= \int_2^x \left(\frac{-\frac{1}{16}}{(x-1)} + \frac{\frac{1}{4}}{(x-1)^2} + \frac{\frac{1}{16}}{(x+3)} \right) dx \\
 \therefore t &= \left[\frac{-1 \ln(x-1)}{16} - \frac{1}{4(x-1)} + \frac{\ln(x+3)}{16} \right]_2^x \\
 &= \left[\frac{1}{16} \ln\left(\frac{x+3}{x-1}\right) - \frac{1}{4(x-1)} \right]_2^x \\
 &= \left(\frac{1}{16} \ln\left(\frac{x+3}{x-1}\right) - \frac{1}{4(x-1)} \right) - \left(\frac{1}{16} \ln\left(\frac{2+3}{2-1}\right) - \frac{1}{4(2-1)} \right) \\
 &= \frac{1}{16} \ln\left(\frac{x+3}{x-1}\right) - \frac{1}{4(x-1)} - \frac{1}{16} \ln(5) + \frac{1}{4} \\
 &= \frac{1}{16} \ln\left(\frac{x+3}{5(x-1)}\right) - \frac{1}{4(x-1)} + \frac{1}{4} \\
 &= \frac{1}{16} \ln\left(\frac{x+3}{5(x-1)}\right) + \frac{1}{4} \left(1 - \frac{1}{x-1} \right) \\
 t &= \frac{1}{16} \ln\left(\frac{x+3}{5(x-1)}\right) + \frac{1(x-2)}{4(x-1)}
 \end{aligned}$$

Motion terminates if x reaches infinity at some finite time if $x \rightarrow \infty$

$$\begin{aligned}
 \frac{x+3}{5(x-1)} &\rightarrow \frac{1}{5}, \quad \frac{1(x-2)}{4(x-1)} \rightarrow \frac{1}{4} \\
 \therefore t &= \frac{1}{16} \ln(1/5) + 1/4
 \end{aligned}$$

≈ 0.1494 time units,
which is certainly finite
 \therefore the motion terminates