

for  $q \neq (2n+1)\pi$ , so  $E < V(q)_{\max}$ , and there are  $q$  turning points given by  $q = 2n\pi \pm \cos^{-1}(-E)$  ( $\pm$  since cosine is an even function). For  $E = -1$ , there is no motion since the only root for  $q$  in the equation  $-1 + \cos q = 0$  is  $q = 2n\pi$  and then  $p = 0$ . Hence all librational motion has  $E$  in the range  $-1 < E < 1$  as required. *No motion for  $E < -1$ .* ✓

$$p^2 = 2(1 + a \sin q)(E + \cos q)$$

$p^2 = (-p)^2$ , so the phase curves are symmetrical under reflection in the  $q$  axis. There will be a 'shoulder' in the phase curves near the point at which  $(1 + a \sin q)$  is minimum i.e. when  $q = (2n - \frac{1}{2})\pi$  since  $\sin(2n - \frac{1}{2})\pi = -1$ , the extent of which will depend on the value of  $a$ , increasing with increasing  $a$ , but since  $0 < a < 1$ , the phase curves will not touch the  $q$  axis because of this shoulder.

When  $q = (2n + \frac{1}{2})\pi$ ,  $\sin q$  is  $\max (= 1)$  and the maximum for  $|p|$  is shifted right with greater values of  $a$ , from  $2n\pi$ , and the maximum for  $p$  is also shifted right with increasing  $E$ . The maximum for  $|p|$  is shifted right with increasing  $a$  because of the phase difference of  $\pi/2$  between  $\cos$  and  $\sin$ . This phase difference also explains the asymmetry in the graph of  $p$  around the  $p$  axis;  $\cos$  and ✓