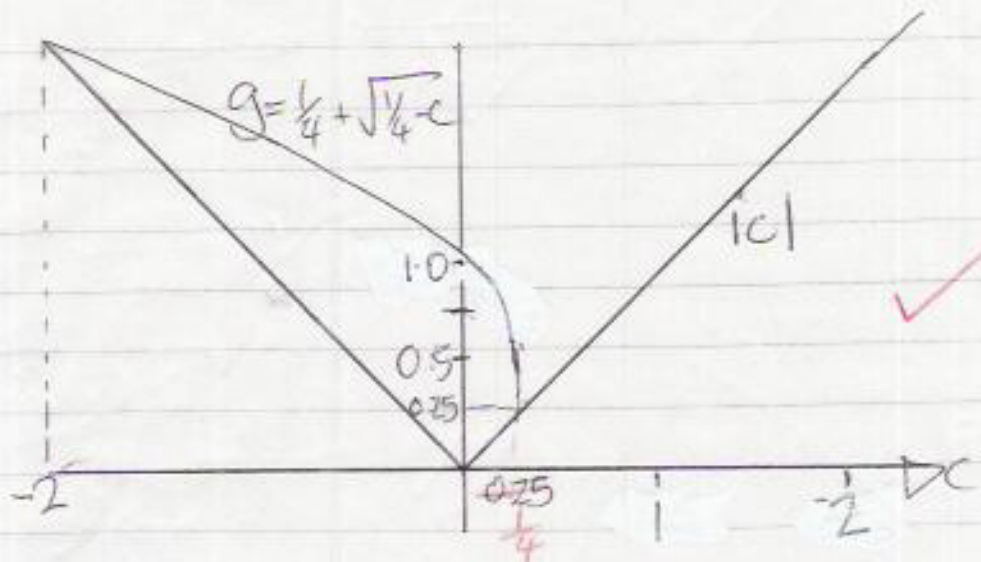


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3)b)



On  $[-2, 1/4]$   $g \geq |c|$ , and since  $f_c(0) = c$

$$|f_c(0)| \leq 1/2 + \sqrt{1/4 - c}$$

Let  $z \in [-1/2 - \sqrt{1/4 - c}, 1/2 + \sqrt{1/4 - c}]$   
Then  $z^2 \in [0, 1/2 - c + \sqrt{1/2 - c}]$

and  $z^2 + c \in [c, 1/2 + \sqrt{1/2 - c}]$

$$|c| \leq 1/2 + \sqrt{1/4 - c}$$

$$\Rightarrow -1/2 + \sqrt{1/2 - c} \leq c \text{ for } c \in [-2, 0]$$

$$\text{for } c \in [0, 1/4] \quad |c| \leq 1/4 \leq 1/2 + \sqrt{1/4 - c}$$

$$\Rightarrow z^2 + c \in [-1/2 - \sqrt{1/2 - c}, 1/2 + \sqrt{1/2 - c}] = I$$

so  $f_g(z)$  maps the interval to itself, so  $|f_c^k(0)|$  is bounded as  $k \rightarrow \infty$  (since  $f_c(0) = c \in I$ ) and  $c \in M$ .

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c) since  $f^n(z) = f(f^{n-1}(z))$  we can write  $z_{n+1} = f(z_n)$   
 $= 3z_n^2 + 2iz_n + (1-i)/3$   
 $3z_{n+1} = 9z_n^2 + 6iz_n + (1-i)$