

Let $S = S_1 \cup S_2 \cup S_3$

$$S([0, 1]) = [0.2, 0.3] \cup [0.5, 0.6] \cup [0.10, 0.11] \text{ (expanded mod 6)}$$

$$S^2([0, 1]) = [0.22, 0.23] \cup [0.25, 0.26] \cup [0.2, 10, 0.2, 11]$$

$$\cup [0.5, 13, 0.5, 14] \cup [0.5, 10, 0.5, 11] \cup [0.55, 0.56]$$

$$\cup [0.62, 0.63] \cup [0.105, 0.10, 6] \cup [0.1010, 0.1011]$$

$$S^3([0, 1]) = [0.222, 0.223] \cup [0.225, 0.226] \cup [0.22, 10, 0.22, 11]$$

$$\cup [0.5, 10, 2] \cup [0.5, 10, 5, 0.5, 10, 6] \cup [0.5, 10, 10, 0.5, 10, 11]$$

$$\cup [0.10, 10, 2, 0.10, 10, 3] \cup [0.10, 10, 5, 0.10, 10, 6] \cup [0.10, 10, 10, 0.10, 10, 11]$$

At stage S^k , we have 3^k intervals of length 16^{-k} from a point whose decimal expansion consists solely of the numbers 2, 5, 10. Note that whatever the decimal expansion of $x \in [0, 1]$, $x = 0.a_1 a_2 \dots$

$$S_1(x) = 0.2 a_1 \dots$$

$$S_2(x) = 0.5, (15 - a_1), (15 - a_2) \dots$$

$$S_3(x) = 0.10 a_1 a_2 \dots$$

$$\text{So } S_{i_1 i_2 i_3 i_4 \dots i_k}(x) = 0.b_1 b_2 b_3 \dots b_k$$

Where b_i is one of 2, 5 or 10.