

(6)

$$= (a, b, c) \begin{pmatrix} 2 & 1 & 2 \\ 1 & 2 & 2 \\ 2 & 2 & 3 \end{pmatrix}$$

$$\text{and } e^1 = (1, 0, 0)^T$$

$$(a, b, c) = (1, 0, 0) \begin{pmatrix} 2 & 1 & 2 \\ 1 & 2 & 2 \\ 2 & 2 & 3 \end{pmatrix}^{-1}$$

With similar expressions to find e^2 and e^3 :

$$\begin{pmatrix} 2 & 1 & 2 & 1 & 0 & 0 \\ 1 & 2 & 2 & 0 & 1 & 0 \\ 2 & 2 & 3 & 0 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 1/2 & 1 & 1/2 & 0 & 0 \\ 1 & 2 & 2 & 0 & 1 & 0 \\ 2 & 2 & 3 & 0 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 1/2 & 1 & 1/2 & 0 & 0 \\ 0 & 3/2 & 1 & -1/2 & 1 & 0 \\ 0 & 1 & 1 & -1 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 1/2 & 1 & 1/2 & 0 & 0 \\ 0 & 1 & 2/3 & -1/3 & 2/3 & 0 \\ 0 & 1 & 1 & -1 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 2/3 & 2/3 & -1/3 & 0 \\ 0 & 1 & 2/3 & -1/3 & 2/3 & 0 \\ 0 & 0 & 1/3 & -2/3 & -2/3 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 0 & 2 & 1 & -2 \\ 0 & 0 & 0 & 1 & 2 & -2 \\ 0 & 0 & 1/3 & -2/3 & -2/3 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 0 & 2 & 1 & -2 \\ 0 & 1 & 0 & 1 & 2 & -2 \\ 0 & 0 & 1 & -2 & -2 & 3 \end{pmatrix}$$

$$\text{so } (a, b, c) = (1, 0, 0) \begin{pmatrix} 2 & 1 & 2 \\ 1 & 2 & 2 \\ -2 & 2 & 3 \end{pmatrix}^{-1}$$