

$$\begin{aligned}
 &= \left((1 + \xi_1^4 + \xi_2^4 - 2\xi_1^2 + 2\xi_2^2 - 2\xi_1^2\xi_2^2 + 4\xi_1^2\xi_2^2 + 4\xi_1^2)^{1/2} \right. \\
 &\times \left. (4\xi_1^2\xi_2^2 + 1 + \xi_1^4 + \xi_2^4 + 2\xi_1^2 - 2\xi_2^2 - 2\xi_1^2\xi_2^2 + 4\xi_1^2\xi_2^2)^{1/2} \right) \\
 &= \left((1 + \xi_1^4 + \xi_2^4 + 2\xi_1^2 + 2\xi_1^2\xi_2^2 + 2\xi_2^2)^{1/2} \right. \\
 &\times \left. (1 + \xi_1^4 + \xi_2^4 + 2\xi_1^2\xi_2^2 + 2\xi_1^2 + 2\xi_2^2)^{1/2} \right) \\
 &= (1 + \xi_1^2 + \xi_2^2)^2
 \end{aligned}$$

$$\therefore n = \frac{V_1 \times V_2}{|V_1| |V_2|} = \frac{2\xi_1}{(1 + \xi_1^2 + \xi_2^2)^{1/2}} \frac{2\xi_2}{(1 + \xi_1^2 + \xi_2^2)^{1/2}} \frac{(\xi_1^2 + \xi_2^2 - 1)}{(1 + \xi_1^2 + \xi_2^2)^{1/2}}$$

$$\frac{\partial n}{\partial \xi_1} = \left(\frac{2(1 + \xi_1^2 + \xi_2^2) - 4\xi_1^2}{(1 + \xi_1^2 + \xi_2^2)^2}, \frac{-4\xi_1\xi_2}{(1 + \xi_1^2 + \xi_2^2)^2}, \frac{(1 + \xi_1^2 + \xi_2^2) \cdot 2\xi_1 - (\xi_1^2 + \xi_2^2 - 1) \cdot 2\xi_1}{(1 + \xi_1^2 + \xi_2^2)^2} \right)$$

$$= \left(\frac{2(1 + \xi_1^2 - \xi_2^2)}{(1 + \xi_1^2 + \xi_2^2)^2}, \frac{-4\xi_1\xi_2}{(1 + \xi_1^2 + \xi_2^2)^2}, \frac{4\xi_1}{(1 + \xi_1^2 + \xi_2^2)^2} \right)$$

$$\frac{\partial n}{\partial \xi_2} = \left(\frac{-4\xi_1\xi_2}{(1 + \xi_1^2 + \xi_2^2)^2}, \frac{2(1 + \xi_1^2 + \xi_2^2) - 4\xi_2^2}{(1 + \xi_1^2 + \xi_2^2)^2}, \frac{(1 + \xi_1^2 + \xi_2^2) \cdot 2\xi_2 - (\xi_1^2 + \xi_2^2 - 1) \cdot 2\xi_2}{(1 + \xi_1^2 + \xi_2^2)^2} \right)$$

$$= \left(\frac{-4\xi_1\xi_2}{(1 + \xi_1^2 + \xi_2^2)^2}, \frac{2(1 + \xi_1^2 - \xi_2^2)}{(1 + \xi_1^2 + \xi_2^2)^2}, \frac{4\xi_2}{(1 + \xi_1^2 + \xi_2^2)^2} \right)$$

The diagonal entries of the Weingarten map are given by $\langle V_1, \partial n / \partial \xi_1 \rangle$ and $\langle V_2, \partial n / \partial \xi_2 \rangle$ times a constant see opp.

$$\langle V_1, \partial n / \partial \xi_1 \rangle = \frac{2(1 - (\xi_1^2 - \xi_2^2))}{(1 + \xi_1^2 + \xi_2^2)^2} - 2\xi_1\xi_2^2, \frac{4\xi_1}{2\xi_1}$$

$$= \frac{2(1 - (\xi_1^2 - \xi_2^2)) - 4\xi_1\xi_2^2}{(1 + \xi_1^2 + \xi_2^2)^2} + \frac{4\xi_1}{(1 + \xi_1^2 + \xi_2^2)^2}$$

$$= \frac{2(1 - \xi_1^2 + \xi_2^2) - 4\xi_1\xi_2^2 + 4\xi_1^2}{(1 + \xi_1^2 + \xi_2^2)^2} = \frac{2 + 2\xi_1^4 + 2\xi_2^4 - 4\xi_1^2 + 4\xi_2^2 - 4\xi_1^2\xi_2^2 + 2\xi_1^2\xi_2^2 + 2\xi_1^2}{(1 + \xi_1^2 + \xi_2^2)^2}$$