

$$g(X_1 + X_2)g^+ = gX_1g^+ + gX_2g^+ \\ g(rX)g^+ = rgXg^+ = r(gXg^+) \text{ for } r \in \mathbb{R} \\ \therefore gXg^+ \text{ is a linear mapping.}$$