

ii) $\det(I+A) \neq 0 \Rightarrow (I+A)^{-1}$ exists and is of same order as A (i.e. $n \times n$).
 $I-A$ is an $n \times n$ matrix.
 $(I-A)(I+A)^{-1}$ is defined, and is an $n \times n$ matrix.

For any orthogonal matrix B , $B^{-1} = B^T$

$$I + A^T A = I + A^T A$$

$$I + (A + A^T) + A^T A = I - (A^T + A) + A^T A$$

$$(I + A^T)(I + A) = (I - A^T)(I - A)$$

$$(I + A^T)^T (I + A) = (I - A^T)^T (I - A)$$

Multiply on left by $((I + A)^T)^{-1}$

on right by $(I - A)^{-1}$

$$(I + A)(I - A)^{-1} = ((I + A)^T)^{-1} (I - A)^T ((I + A)^T)^{-1} (I - A)$$

By properties of inverse and transposition.

$$(I - A)(I + A)^{-1} = ((I - A)(I + A)^{-1})^T$$