

0001101	0001101	0001101
8	8	1
0000101	0000101	0000001
1	2	3
0000001	0000001	00000010
4	5	5
00000011	00000011	00000011
6	6	6
00000011	00000011	00000011 ✓
7	9	9

- iii/a)  $f(2) = 1$  (finishing in state 9)  
 $f(4) = 2$  (finishing in state 9)  
 $f(5) = 2$  (finishing in state 10)  
 $f(6) = 3$  (finishing in state 9)  
 $f(9) = 4$  (finishing in state 10)

b) In general (like a fool I worked out  $f(5)$ ,  $f(6)$  and  $f(9)$  to be sure) *good*.

$$f(n) = \begin{cases} \frac{n}{2} & \text{if } n \text{ is even, finishing in state 9.} \\ \frac{n-1}{2} & \text{if } n \text{ is odd, finishing in state 10.} \end{cases}$$

Starting in state 1, the machine erases two 1s between states 1 and 3 (unless  $n=1$ , in which case it erases a 1 in state 1 and moves through state 2 to state 10, then stops, then moves to the right most end of the block of 1s, and one space more, in state 4. In moving to state 5 it moves right one more space. If there is a one there (the machine is designed to store  $\frac{1}{2}$  the no of ones it has subtracted from