

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} R_1 \rightarrow R_1 - 3R_2 \quad 2/2$$

Which is just the matrix representing  $D$ .  $D$  and  $E$  are isomorphic. This is so because  $T$  can be expressed as the identity matrix using row and column operations. It's the case that any matrix whose determinant is one can be reduced to the identity matrix: instead of  $T$ , any  $3 \times 3$  matrix whose determinant is one would have given the same result.  $2/2$

24/25

$$2) 3675 = 3 \times 5^2 \times 7^2 \quad \checkmark 1/1$$

prime power	factors of $d_{k-1}$	$d_k$
$7^2$	7	$7^2$
$5^2$	5	$5^2$
3	3	3

$\checkmark 2/2$

There  $2 \times 2 \times 1 = 4$  Abelian groups order 3675. If we call these  $A, B, C, D$ , there are

$$A \cong (\mathbb{Z}_3) \times (\mathbb{Z}_{25}) \times (\mathbb{Z}_{49}) \cong \mathbb{Z}_{3675}$$

$$B \cong (\mathbb{Z}_3) \times (\mathbb{Z}_5 \times \mathbb{Z}_5) \times (\mathbb{Z}_{49}) \cong \mathbb{Z}_5 \times (\mathbb{Z}_3 \times \mathbb{Z}_5 \times \mathbb{Z}_{49})$$

$$\cong \mathbb{Z}_5 \times \mathbb{Z}_{735}$$

$$C \cong (\mathbb{Z}_3) \times (\mathbb{Z}_{25}) \times (\mathbb{Z}_7 \times \mathbb{Z}_7) \cong \mathbb{Z}_7 \times (\mathbb{Z}_3 \times \mathbb{Z}_7 \times \mathbb{Z}_{25})$$

$$\cong \mathbb{Z}_7 \times \mathbb{Z}_{525}$$

$$D \cong (\mathbb{Z}_3) \times (\mathbb{Z}_5 \times \mathbb{Z}_5) \times (\mathbb{Z}_7 \times \mathbb{Z}_7) \cong (\mathbb{Z}_5 \times \mathbb{Z}_7) \times (\mathbb{Z}_3 \times \mathbb{Z}_5 \times \mathbb{Z}_7)$$

$$\cong \mathbb{Z}_{35} \times \mathbb{Z}_{105}$$

4/4

The primary decomposition follows the 1st sign  $\checkmark$