

A member of the set, \cdot is for this set

The Cayley table

X_{24}	1	5
1	1	5
5	5	1

so the set is closed. All the subgroup axioms are satisfied, so $\{1, 5\}$ is a subgroup under the operation multiplication modulus 24.

Consider $\{1, 5, 7, 13\}$. From the Cayley table this set is closed. Each element is self inverse so has an inverse which is a member of the set. The identity is a member of the set. All the subgroup axioms are satisfied, so the set is a subgroup under multiplication modulus 24, and the Group G has a subgroup of order 4, $\{1, 5, 7, 13\}$.

Also every Group G has as a subgroup the group G itself, so G has a subgroup of order 8.

b) $H = \{1, 5\}$
 $7H = \{7, 13\}$
 $13H = \{13, 17\}$
 $19H = \{19, 23\}$

$H = \{1, 5\}$
 $H7 = \{7, 13\}$
 $H13 = \{13, 17\}$
 $H19 = \{19, 23\}$

The left and right cosets of H are the same hence the subgroup H is normal in G .

Alternatively, multiplication is commutative, hence the group G is Abelian, so H is normal in G . The Cayley table is symmetric about the main diagonal, so the group can be identified as Abelian by this route.

This better reason.