

now on their domains. Also  $f(0 - \frac{1}{n}) = f(-\frac{1}{n}) = (-\frac{1}{n})^3 \rightarrow 0$  as  $n \rightarrow \infty$ , and  $f(0) = \sin(2 \cdot 0) = 0$ , hence  $f(x_n) \rightarrow f(0)$  where  $x_n \rightarrow 0$ , and the function is continuous at 0. Need glue Rule here.

On  $[\pi, \infty[$ ,  $f(x) = e^{-x}$ , an exponential function which is differentiable, hence continuous on  $[\pi, \infty[$ . We have already shown that  $f(x)$  is discontinuous at  $\pi$ , and just shown that  $f(x)$  is continuous at any other point of  $\mathbb{R}$  hence  $f(x)$  is continuous on  $\mathbb{R} - \{\pi\}$ . Need Local Rule for  $]0, \pi[$  and  $]\pi, \infty[$  also

5)  $G = \{1, 5, 7, 11, 13, 17, 19, 23\}$

a)  $G$  might be has subgroups of possible order 1, 2, 4, 8 (these numbers are whole divisors of the order of  $G$ ).

A subgroup of order 1 is the identity element  $e$ , i.e.  $\{1\}$ . 5/8

The Group  $G$  has Cayley table

$x_{24}$	1	5	7	11	13	17	19	23
1	1	5	7	11	13	17	19	23
5	5	1	11	7	17	13	23	19
7	7	11	1	5	19	23	13	17
11	11	7	5	1	23	19	17	13
13	13	17	19	23	1	5	7	11
17	17	13	23	19	5	1	11	7
19	19	23	13	17	7	11	1	5
23	23	19	17	13	11	7	5	1

From the Cayley table, every element is self inverse, so a subgroup of order 2 could consist of the identity, 1, and any other element e.g.  $\{1, 5\}$ . The identity is a member of this set and each element of the set is self inverse, so has an inverse which is