

$$(1+3x^5)^{2/11} = 1 + \frac{2}{11} \cdot 3x^5 + \frac{2}{11} \cdot \frac{7}{11} \cdot \frac{-4}{11} \cdot (3x^5)^2 + \frac{2}{11} \cdot \frac{7}{11} \cdot \frac{-4}{11} \cdot \frac{-15}{11} \cdot (3x^5)^3 + \dots$$

$$\stackrel{24/25}{=} 1 + \frac{21}{11}x^5 - \frac{126}{121}x^{10} + \frac{1890}{1331}x^{15} \dots$$

$\frac{24}{25} \times \frac{1}{6} = \frac{4}{5}$

This particular series converges for all x . Formally the series converges for $|x| < \infty$.
 $-\infty < x < \infty$ X Valid for $|3x^5| < 1$ i.e. $R = (\frac{1}{3})^{1/5}$

4) $V(x, y) = (5x - 2y, 7x - 4y)$ $((x, y) \in \mathbb{R}^2)$

a) i) $A = \begin{pmatrix} 5 & -2 \\ 7 & -4 \end{pmatrix}$ ✓

ii) $\det(A) = -6$ $\text{tr}(A) = +1$

$u''(t) - u'(t) - 6u(t) = 0$ ✓ 24

where $u(t)$ may be either of the coordinate functions $f(t)$ or $g(t)$ of the flow function

b) i) $V(1, 0) = \begin{pmatrix} 5 & -2 \\ 7 & -4 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 5 \\ 7 \end{pmatrix}$

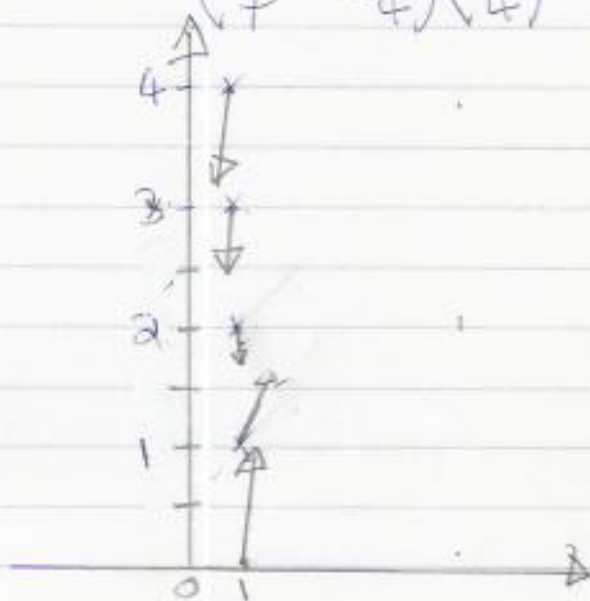
$V(1, 1) = \begin{pmatrix} 5 & -2 \\ 7 & -4 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 3 \\ 3 \end{pmatrix}$ ✓

$V(1, 2) = \begin{pmatrix} 5 & -2 \\ 7 & -4 \end{pmatrix} \begin{pmatrix} 1 \\ 2 \end{pmatrix} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$ ✓

$V(1, 3) = \begin{pmatrix} 5 & -2 \\ 7 & -4 \end{pmatrix} \begin{pmatrix} 1 \\ 3 \end{pmatrix} = \begin{pmatrix} -1 \\ -5 \end{pmatrix}$ ✓

$V(1, 4) = \begin{pmatrix} 5 & -2 \\ 7 & -4 \end{pmatrix} \begin{pmatrix} 1 \\ 4 \end{pmatrix} = \begin{pmatrix} -3 \\ -9 \end{pmatrix}$ ✓

ii)



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✓