

$$= x(-1) - y(1) + z(2-a+a)$$

$$= -x - y + 2z = 0 \quad \text{or} \quad x + y - 2z = 0.$$

e)  $(1, 1, 1)$  is a solution of  $x + y - 2z = 0$  hence line passes through  $u$ .

To find the cross ratio  $(ABCu)$

$$A(1, -1, 0)$$

$$B(2a-1, 1, a)$$

$$C(a, 2-a, 1)$$

$$u(1, 1, 1)$$

solve  $C = \alpha A + \beta B$

$$\begin{pmatrix} a \\ 2-a \\ 1 \end{pmatrix} = \alpha \begin{pmatrix} 1 \\ -1 \\ 0 \end{pmatrix} + \beta \begin{pmatrix} 2a-1 \\ 1 \\ a \end{pmatrix}$$

$$a = \alpha + \beta(2a-1) \quad (1)$$

$$2-a = -\alpha + \beta \quad (2)$$

$$1 = a\beta \quad (3)$$

From (3)  $\beta = 1/a$

Sub  $\beta = 1/a$  into (2),  $\alpha = \beta - 2 + a$   
 $= 1/a - 2 + a = (a^2 - 2a + 1)/a$

check from (1)  $\alpha = a - \beta(2a-1)$   
 $= a - (2a-1)/a$   
 $= (a^2 - 2a + 1)/a$

solve  $u = \gamma A + \delta B$

$$\begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = \gamma \begin{pmatrix} 1 \\ -1 \\ 0 \end{pmatrix} + \delta \begin{pmatrix} 2a-1 \\ 1 \\ a \end{pmatrix}$$

$$1 = \gamma + \delta(2a-1) \quad (1)$$

$$1 = -\gamma + \delta \quad (2)$$

$$1 = a\delta \quad (3)$$

From (3)  $\delta = 1/a$

Sub  $\delta = 1/a$  into (2)

$$1 = -\gamma + 1/a \Rightarrow \gamma = 1/a - 1 = (1-a)/a$$

check from (1)  $\gamma = 1 - \delta(2a-1)$   
 $= 1 - (2a-1)/a = (a - 2a + 1)/a$   
 $= (1-a)/a$