

$$M(2-i)=0=K((2-i)-m) \Rightarrow m=2-i$$

$$M(1+3i)=1=K((1+3i)-(2-i))$$

$$1=K(-1+4i)=K \frac{(-1+4i)(-1-4i)}{(-1-4i)}$$

$$(-1-4i)=K(17)$$

$$K=(-1-4i)/17$$

$$M(z)=\frac{(-1-4i)}{17}(z-2+i)$$

check $M(2-i)=0$

$$M(1+3i)=\frac{(-1-4i)}{17}(1+3i-2+i)=\frac{(-1-4i)(-1+4i)}{17}$$

$$=1$$

If $z_3 = -1/2 + 9i$ is collinear with z_1 and z_2
 $M(z)$ will map z_3 to the real axis.

$$M(-1/2+9i)=\frac{(-1-4i)}{17}(-1/2+9i-2+i)$$

$$=\frac{(-1-4i)}{17}(-5/2+10i)$$

$$=\frac{(-1-4i)(-5+20i)}{34}=\frac{1(5-20i+20i+80)}{34}$$

$$=\frac{85}{34}=5/2$$

$$\left(\frac{23}{2}\right)$$

$M(z_3)$ is real so z_1, z_2 and z_3 are collinear. ✓

$$3) K: x^2+y^2+x-y+7/16=0$$

$$\text{equivalently } (x+1/2)^2+(y-1/2)^2=1/16$$

K is a circle with centre $(-1/2, 1/2)$, radius $1/4$.
 In the complex plane K is a circle with
 centre $\alpha = -1/2 + i/2$, radius $= 1/4$. In the complex
 plane therefore, K is a circle such that

$$K = \{z: |z - (-1/2 + i/2)| = 1/4\}$$

✓

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