

then $y = \frac{1}{3}$, so $y = \frac{x}{3} + \frac{1}{3}$.
 Consider AP. We have two points through which AP passes, for both of which $x=0$.
 Hence this is the equation of AP.
 Since X lies on AP and BQ, which has equation $y = \frac{x}{3} + \frac{1}{3}$, we can substitute $x=0$ into the equation for BQ to find the y coordinate of X. Hence the coordinates of X are $(0, \frac{1}{3})$. 3/3

$$\begin{aligned} BX &= |X-B| = |(0, \frac{1}{3}) - (-1, 0)| = |(1, \frac{1}{3})| = \sqrt{1^2 + (\frac{1}{3})^2} = 2 \\ XQ &= |Q-X| = |(\frac{1}{2}, \frac{1}{2}) - (0, \frac{1}{3})| = |(\frac{1}{2}, \frac{1}{6})| = \sqrt{(\frac{1}{2})^2 + (\frac{1}{6})^2} = 1 \\ AX &= |X-A| = |(0, \frac{1}{3}) - (0, 0)| = |(0, \frac{1}{3})| = \frac{1}{3} \\ XP &= |P-X| = |(0, 0) - (0, \frac{1}{3})| = |(0, -\frac{1}{3})| = \frac{1}{3} \end{aligned}$$

but see unit 1, p 35 for a quicker method of getting ratios

By the Fundamental Theorem of Affine Geometry, given any arbitrary triangle $A'B'C'$, there is an affine transformation that sends A' to A , B' to B and C' to C respectively. Affine transformations preserve ratios of lengths, and since in the triangle ABC , $\frac{BX}{XQ} = \frac{AX}{XP} = 2$, so along straight lines

the same ratios will apply in the triangle $A'B'C'$. The same applies for the inverse transformation that maps ABC to $A'B'C'$. Hence if $\frac{B'X'}{X'Q'} = 2$, $\frac{B'X'}{B'Q'} = \frac{2}{3}$, and if $\frac{A'X'}{X'P'} = 2$, $\frac{A'X'}{A'P'} = \frac{2}{3}$ and $\frac{B'X'}{B'Q'} = \frac{2}{3}$ and $\frac{A'X'}{A'P'} = \frac{2}{3}$.
 Verify that X ~~also~~ ~~lies on~~ ~~CE~~.
 division CE is also 2:1.
 for given triangle.

c) Affine transformations have the form

$$T(x) = Ax + b$$

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