

From the Cayley table, the subgroup is cyclic generated by (124635) . It is therefore isomorphic to any cyclic group of order 6 eg (\mathbb{Z}_6^+) .
The Cayley table for (\mathbb{Z}_6^+) is

$+_6$	0	1	2	3	4	5
0	0	1	2	3	4	5
1	1	2	3	4	5	0
2	2	3	4	5	0	1
3	3	4	5	0	1	2
4	4	5	0	1	2	3
5	5	0	1	2	3	4

This group is cyclic, generated by 1. An isomorphism is found by matching corresponding powers of ρ and (124635) under their respective compositions.

The isomorphism is then

$$(124635) \mapsto \rho$$

$$(143265) \mapsto \rho^2$$

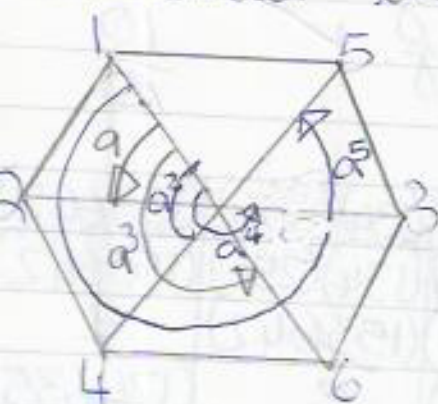
$$(16)(23)(45) \mapsto \rho^3$$

$$(134)(256) \mapsto \rho^4$$

$$(153642) \mapsto \rho^5$$

$$(1)(2)(3)(4)(5)(6) = e \mapsto \rho^0$$

Also consider the hexagon, labelled as shown.



an isomorphism is then

$$(124635) \mapsto \rho = a$$

$$(143265) \mapsto \text{rotation anticlockwise about } \frac{2\pi}{3} = a^2$$

$$(16)(23)(45) \mapsto \text{rotation about } \pi \text{ anticlockwise} = a^3$$

$$(134)(256) \mapsto \text{rotation anticlockwise about } \frac{4\pi}{3} = a^4$$

$$(153642) \mapsto \text{rotation anticlockwise about } \frac{5\pi}{3} = a^5$$

$$(1)(2)(3)(4)(5)(6) \mapsto \text{rotation about } 2\pi \text{ anticlockwise} = e$$

The isomorphism is then to the set of rotations of a hexagon, irregularly labelled.