

$$d) i) P(X) = \frac{n!}{x!(n-x)!} p^x (1-p)^{n-x}$$

$$P_S(0) = \frac{20!}{0!(20-0)!} 0.08^0 (1-0.08)^{20-0} = 0.92^{20} = 0.1887$$

$$P_H(0) = \frac{20!}{0!(20-0)!} 0.01^0 (1-0.01)^{20-0} = 0.99^{20} = 0.8179$$

$\frac{2}{2}$

ii) To complete the table

$$P_S(1) = \frac{20!}{1!19!} \times 0.08 \times 0.92^{19} = 0.3282$$

$$P_S(2) = \frac{20!}{2!18!} \times 0.08^2 \times 0.92^{18} = 0.2711$$

$$P_S(3) = \frac{20!}{3!17!} \times 0.08^3 \times 0.92^{17} = 0.1414$$

$$P_S(4) = \frac{20!}{4!16!} \times 0.08^4 \times 0.92^{16} = 0.0523$$

$$P_S(X > 4) = 1 - (P(0) + P(1) + P(2) + P(3) + P(4)) \\ = 1 - (0.3282 + 0.2711 + 0.1414 + 0.0523) \\ = 1 - 0.793 = 0.207$$

And for the high quality boxes

$$P_H(1) = \frac{20!}{1!19!} \times 0.01 \times 0.99^{19} = 0.1652$$

$$P_H(2) = \frac{20!}{2!18!} \times 0.01^2 \times 0.99^{18} = 0.0159$$

$$P_H(3) = \frac{20!}{3!17!} \times 0.01^3 \times 0.99^{17} = 0.001$$

$$P_H(4) = \frac{20!}{4!16!} \times 0.01^4 \times 0.99^{16} = 0 \text{ (to four significant digits)}$$

$$P_H(X > 4) = 1 - (P(0) + P(1) + P(2) + P(3) + P(4)) \\ = 1 - (0.1652 + 0.0159 + 0.001 + 0) = 0.8179$$

Now we can complete the table (on next page)