

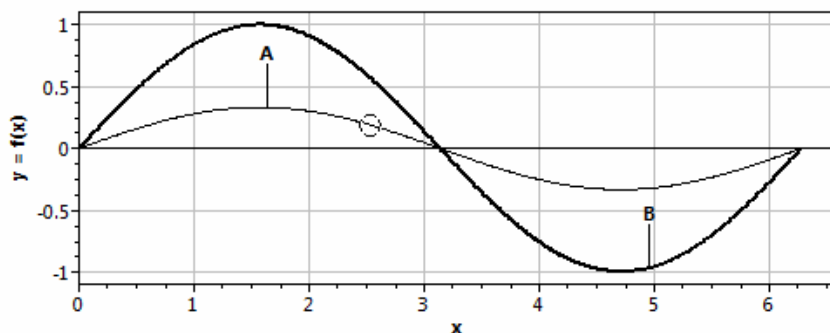
IB – SL Math Portfolio
Jonathan

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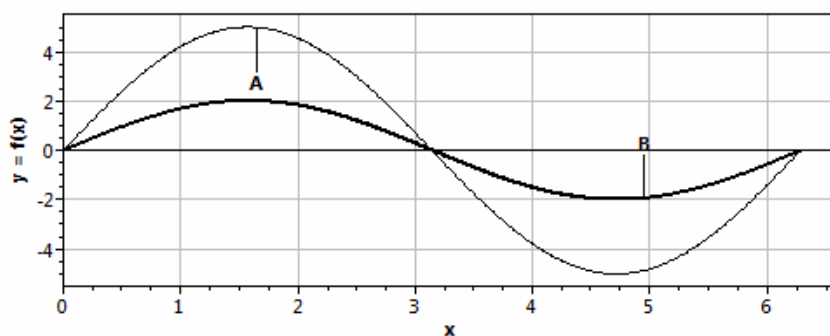
Investigating the graphs of sine function

In this investigation, we are going to look at the different graph of $y = \sin x$. We are going to compare and investigate the graphs of $y = A \sin x$, $y = \sin Bx$ and $y = \sin(x+C)$. We are going to look what the different value and what are the effects on the sine graph.

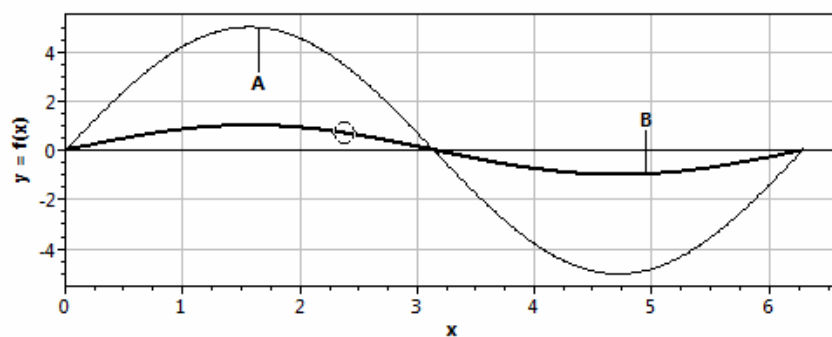
Part 1: Investigation of the graphs $y = \sin x$



A. $y = 1/3 * \sin x$
B. $y = 1 * \sin x$



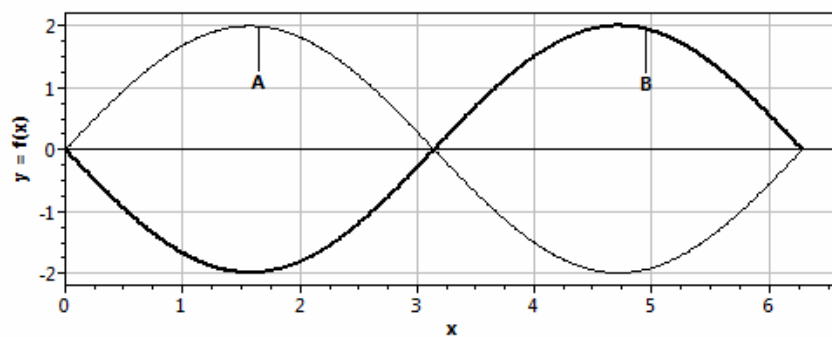
A. $y = 5 * \sin x$
B. $y = 2 * \sin x$



A. $y = 5 \cdot \sin x$

B. $y = 1 \cdot \sin x$

In the graphic $5 \sin x$, as you can see is much stretched because the amplitude is greater in $5 \sin x$ than $2 \sin x$. But you can also see that in $2 \sin x$, the graph is much wider the $5 \sin x$. So we can conclude that more the amplitude is low and more the graph is wide.

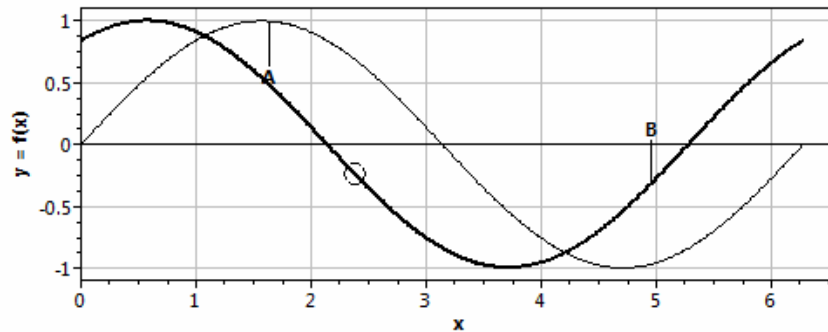


A. $y = 2 \cdot \sin x$

B. $y = -2 \cdot \sin x$

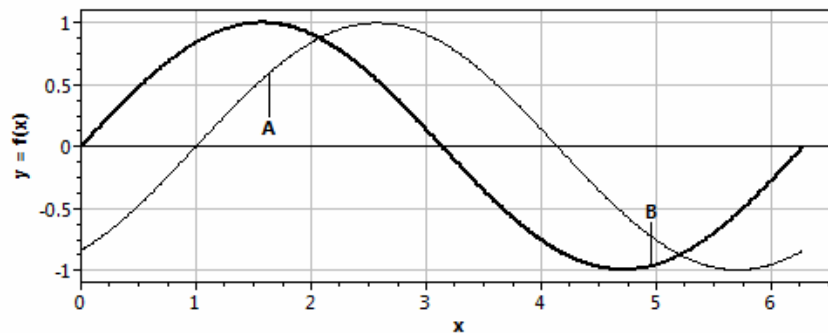
I put $-2 \sin x$ to show that when the value of the amplitude is negative, the graph will flip up sat down.

Part 3: Investigation of the graphs $y = \sin(x+C)$



A. $y = \sin x$
B. $y = \sin(x + 1)$

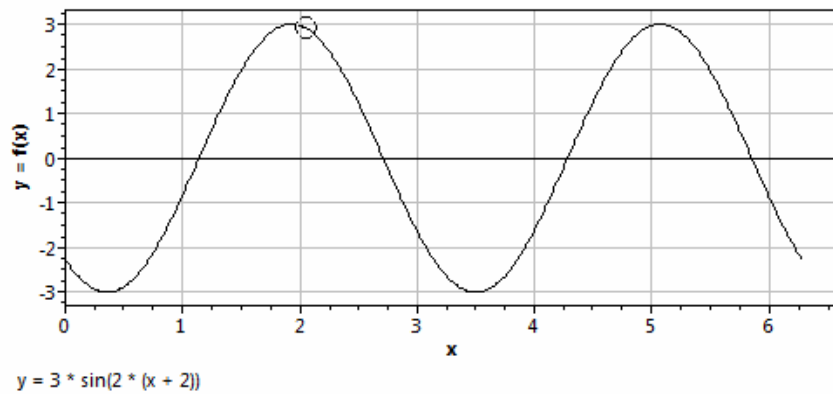
I choose $\sin(x+1)$ and $\sin x$ to show that when the number is positive, the period will move to the left by one because it will start at 1 for the amplitude.



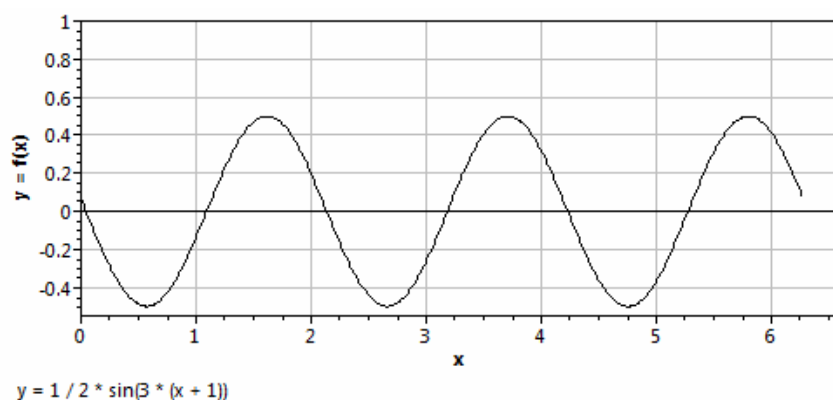
A. $y = \sin(x - 1)$
B. $y = \sin x$

Here you can see that when the value in the parenthesis is negative, the period will shift to the right by one and the amplitude will start at -1.

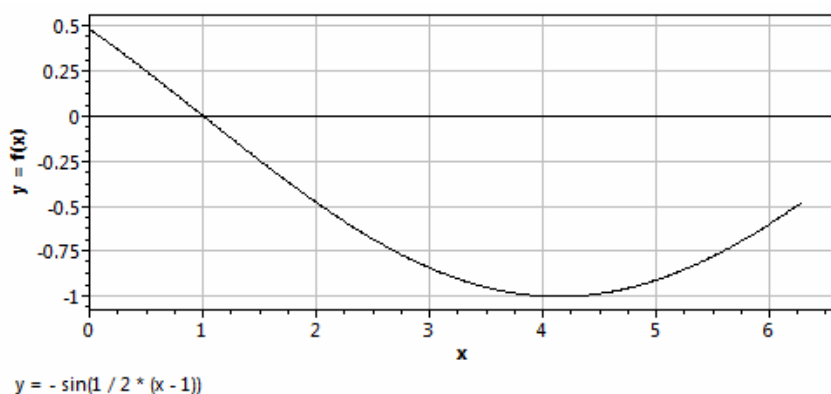
Part 4: Prediction of the shape and position of the graphs



So, based on what I did, I saw that the value of the amplitude was 3 so a positive but I didn't use well the $(x + 2)$ because I thought it would be more far to the left.



For this graph, it was pretty hard to predict, the amplitude is $1/2$ which is positive but because of $+1$, we will move to the left. You can see that I was right for the value B when it says $\sin 3$, I had the right period.



This one I really had a good prediction, I knew that the amplitude would be on 0.5 and since the amplitude is a -1 it would be up sat down but because of the (x-1) the amplitude start at 0.5. I knew as well that the value B in $\sin 1/2$ would be very wide period.

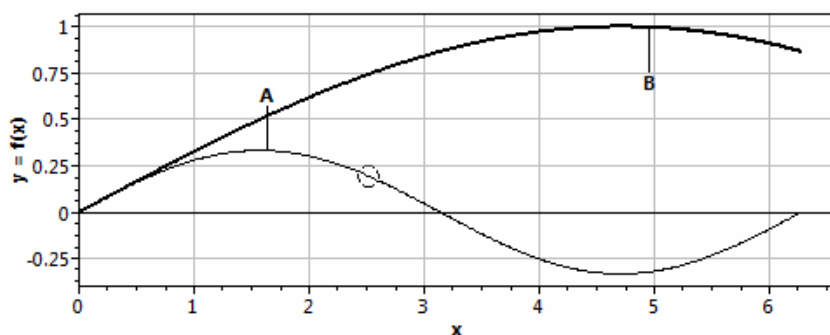
$$Y = \blacktriangle \sin B(x + C)$$

In this graph, there is three different value \blacktriangle , B and C. The value \blacktriangle is the amplitude, if it 1 the amplitude will be 1 but if it's a negative 1, the graph will have to flip up sat down.

The value B it determine the period, so if the value will be $1/2$, the period will be longer therefore it would be wider that for example 3. More the Value B is lower and more the period will be wider.

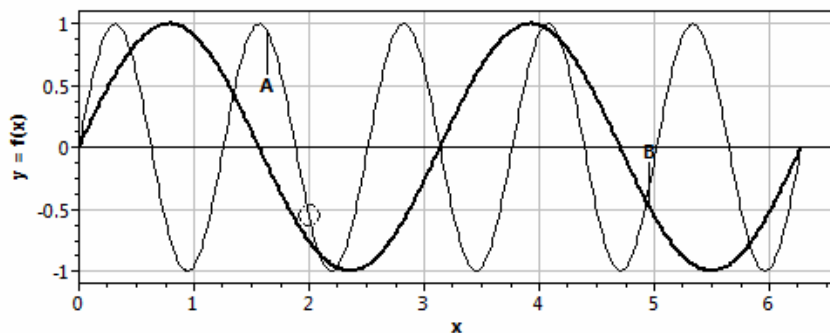
The value C is the one that determine what side you are going to shift the graph, if it is positive it will shift to the left and if it is a negative it will move to the right

Part 2: Investigation of the graphs $y = \sin Bx$



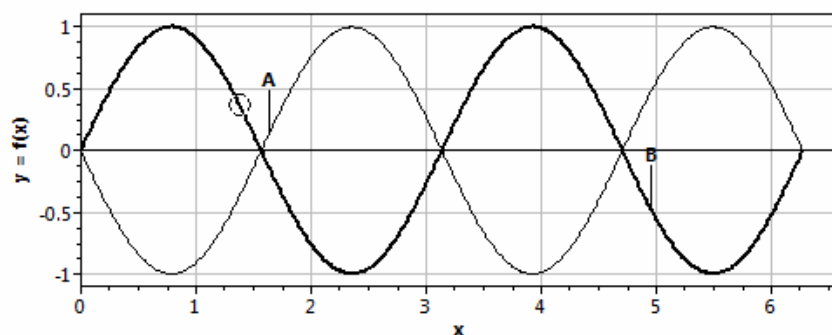
A. $y = \frac{1}{3} \sin x$
B. $y = \sin(\frac{1}{3}x)$

Here we can see that it is very different that $\frac{1}{3} \sin x$. The period on $\sin \frac{1}{3}x$ is much more widely than $\frac{1}{3} \sin x$.



A. $y = \sin(5x)$
B. $y = \sin(2x)$

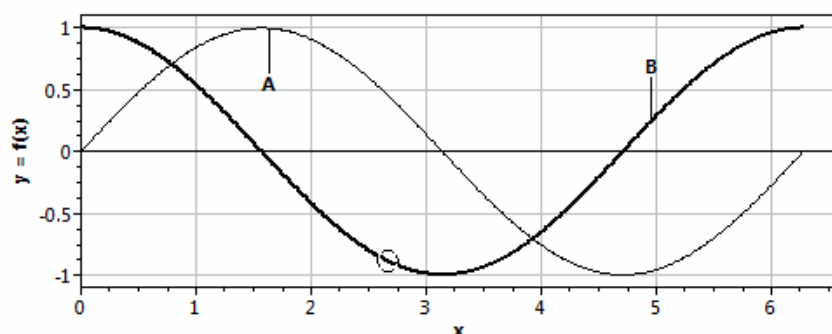
In those graphs, we can clearly see that the period in the graph $\sin 5x$ is shorter than the $\sin 2x$. Therefore more the value of B is lower and more the curve of the graph will be wide. Now let's try with a negative.



A. $y = \sin(-2 \cdot x)$
B. $y = \sin(2 \cdot x)$

Like in the graph $y = \sin x$, if the value of x is a negative, the graph will flip up and down.

Part 5: Investigation of the graphs $y = \cos x$ and $y = \sin x$



A. $y = \sin x$
B. $y = \cos x$

The graphs $\cos x$ is linked to the graph $\sin x$, because it has the same curvy line but it has also the same amplitude which is 1.

But The difference is the location of the relative along the x -axis. For cosine function, you need to think about the unit circle. At a rotation of $\pi/2$ radians, the cosine component of the image is 0. Another $\pi/2$ radians, you go back to 1. A sine function it is one rotation of $\pi/2$ behind the cosine function. So all that's keeping them from being the same function is the difference of $\pi/2$.